

## LIMITES

Comprueba los siguientes límites:

$$1.- \lim_{x \rightarrow \infty} \frac{x^3}{e^x} = 0$$

$$3.- \lim_{x \rightarrow 0} \frac{1}{x} - \frac{1}{\ln(x+1)} = -\frac{1}{2}$$

$$5.- \lim_{x \rightarrow 0} \frac{e^x - 1}{x} = 1$$

$$7.- \lim_{x \rightarrow 0} \operatorname{cosec} x - \frac{1}{x} = 0$$

$$9.- \lim_{x \rightarrow p/2} \frac{\operatorname{tg} x - 3}{\operatorname{sec} x + 1} = 1$$

$$11.- \lim_{x \rightarrow 0} \frac{e^x - e^{\operatorname{sen} x}}{x^3} = \frac{1}{6}$$

$$13.- \lim_{x \rightarrow \infty} (x^3 - 2x + 3)^{\frac{1}{x}} = 1$$

$$15.- \lim_{x \rightarrow p/2} \frac{\operatorname{tg} 3x}{\operatorname{tg} 5x} = \frac{5}{3}$$

$$17.- \lim_{x \rightarrow 0} (\operatorname{sen} x)^x = 1$$

$$19.- \lim_{x \rightarrow \infty} \left( \frac{x^2 + 1}{x^2 - 2x} \right)^{x+2} = e^2$$

$$21.- \lim_{x \rightarrow 0^+} [x (\ln x)^n] = 0$$

$$23.- \lim_{x \rightarrow 0} (\operatorname{sen} x + \operatorname{cos} x)^{\operatorname{cot} g x} = e$$

$$25.- \lim_{x \rightarrow \infty} \frac{\ln x}{\sqrt{x}} = 0$$

$$27.- \lim_{x \rightarrow \infty} \frac{\ln x}{x} = 0$$

$$29.- \lim_{x \rightarrow 0} x^x = 17 \quad \lim_{x \rightarrow 0} \left( \frac{1}{x} \right)^{\operatorname{tg} x} = 1$$

$$2.- \lim_{x \rightarrow I^+} (x^2 - 1) \operatorname{tg} \left( \frac{p}{2} x \right) = -\frac{4}{p}$$

$$4.- \lim_{x \rightarrow 0} \frac{\ln x}{\operatorname{cot} g x} = 0$$

$$6.- \lim_{x \rightarrow 0} \frac{1 - \cos x}{3x^2} = \frac{1}{6}$$

$$8.- \lim_{x \rightarrow 1} \frac{\operatorname{sen}(x - 1)}{x^2 - 3x + 2} = -1$$

$$10.- \lim_{x \rightarrow 3} \left( \frac{2}{x-3} - \frac{12}{x^2-9} \right) = \frac{1}{3}$$

$$12.- \lim_{x \rightarrow p/2} (\operatorname{sen} x)^{\operatorname{tg} x} = 1$$

$$14.- \lim_{x \rightarrow \frac{p}{2}} \frac{(1 + 2 \operatorname{cos} x)^{\frac{1}{\operatorname{cos} x}}}{2} = e^2$$

$$16.- \lim_{x \rightarrow 0} \frac{e^x - e^{-x} - 2x}{x - \operatorname{sen} x} = 2$$

$$18.- \lim_{x \rightarrow 0^+} (\operatorname{tg} x \cdot \ln x) = 0$$

$$20.- \lim_{x \rightarrow 0} \left( \frac{1}{x} - \frac{1}{\operatorname{sen} x} \right) = 0$$

$$22.- \lim_{x \rightarrow \infty} \frac{\ln^4 x}{x^2} + 1 = 1$$

$$24.- \lim_{x \rightarrow \infty} \left( x \ln \frac{1+x}{x} \right) = 1$$

$$26.- \lim_{x \rightarrow 0} \frac{1 - \operatorname{cos} x}{(\operatorname{e}^x - 1)^2} = \frac{1}{2}$$

$$28.- \lim_{x \rightarrow \infty} x (5^{\frac{1}{x}} - 1) = \ln 5$$

$$8.- \lim_{x \rightarrow 1} x^{\frac{1}{x-1}} = \frac{1}{e}$$

9.-  $\lim_{x \rightarrow 1} \left( \frac{x}{x-1} - \frac{1}{\ln x} \right) = \frac{1}{2}$

10.-  $\lim_{x \rightarrow p/2} \cos x \ln(\tan x) = 0$

11.-  $\lim_{x \rightarrow p/4} \tan x^{\frac{1}{\cos 2x}} = \frac{1}{e}$

12.-  $\lim_{x \rightarrow 0^+} x^2 \ln x = 0$

13.-  $\lim_{x \rightarrow \infty} (x^2 + 1)^{\frac{1}{x}} = 1$

14.-  $\lim_{x \rightarrow \infty} \frac{3^x}{x^3} = \infty$

15.-  $\lim_{x \rightarrow 0} \frac{x \cos x - \sin x}{x^3} = -\frac{1}{3}$

16.-  $\lim_{x \rightarrow \infty} (\ln x)^{\frac{1}{x}} = 1$

17.-  $\lim_{x \rightarrow \infty} \left( 1 + \frac{5}{x} \right)^{7x} = e^{35}$

18.-  $\lim_{x \rightarrow 1^+} (x-1) \ln(x-1) = 0$

19.-  $\lim_{x \rightarrow \infty} (\ln x)^{\frac{1}{x^2}} = 1$

20.-  $\lim_{x \rightarrow 0} \frac{\cos x - 2x^2 - 1}{3x^2} = -\frac{5}{6}$

21.-  $\lim_{x \rightarrow 0} \frac{x - \sin x}{\tan x - \sin x} = \frac{1}{3}$

22.-  $\lim_{x \rightarrow 0} \frac{x}{x + \sin x} = \frac{1}{2}$

23.-  $\lim_{x \rightarrow 0} \frac{x^3 \sin x}{(1 - \cos x)^2} = 4$

24.-  $\lim_{x \rightarrow 0} \frac{\sin x}{\tan x} = 1$

25.-  $\lim_{x \rightarrow 0} \ln x \tan x = 0$

26.-  $\lim_{x \rightarrow \infty} \frac{\ln x}{\sqrt[3]{x}} = 0$

27.-  $\lim_{x \rightarrow 0} \left( \frac{1}{\sin^2 x} - \frac{1}{x^2} \right) = \frac{1}{3}$

28.-  $\lim_{x \rightarrow \infty} x \sin \frac{a}{x} = a$

29.-  $\lim_{x \rightarrow 0} \frac{\tan x - \sin x}{x^3} = \frac{1}{2}$

30.-  $\lim_{x \rightarrow 0} (\cos x)^{\cot^2 x} = e^{\frac{1}{2}}$

31.-  $\lim_{x \rightarrow 0} \frac{1 - \cos^2 x}{(\sin x + \tan x)^2} = \frac{1}{4}$

32.-  $\lim_{x \rightarrow 0} \frac{x - \sin 2x}{x + \sin 3x} = -\frac{1}{4}$

33.-  $\lim_{x \rightarrow 0} \frac{\operatorname{arcotg} x - x}{x - \sin x} = -2$

34.-  $\lim_{x \rightarrow 0} \frac{\operatorname{arcotg} x - x - \frac{x^3}{3}}{x^3} = -\frac{2}{3}$

35.-  $\lim_{x \rightarrow 0} \frac{\tan x - x}{x - \sin x} = -1$

36.-  $\lim_{x \rightarrow 0} \left( \frac{a^x + b^x}{2} \right)^{\frac{1}{x}} = a \cdot b$

37.-  $\lim_{x \rightarrow 0} (1 - \cos x)^{\tan x} = 1$

38.-  $\lim_{x \rightarrow 0^+} \frac{\ln x}{\operatorname{cosec} x} = 0$

39.-  $\lim_{x \rightarrow 0} x \cdot \ln x = 0$

40.-  $\lim_{x \rightarrow 1} \left( \frac{1}{\ln x} - \frac{1}{x-1} \right) = \frac{1}{2}$

41.-  $\lim_{x \rightarrow 0} \left( \frac{1}{x} - \frac{1}{e^x - 1} \right) = \frac{1}{2}$

42.-  $\lim_{x \rightarrow -1} \frac{x+1}{\sqrt{6x^2+3} + 3x} = 1$

43.-  $\lim_{x \rightarrow 1} \frac{2x - 2}{(26+x)^{1/3} - 3} = 54$

44.-  $\lim_{x \rightarrow -1} \frac{1+x^{1/3}}{1+x^{1/5}} = \frac{5}{3}$

45.-  $\lim_{x \rightarrow 0} (1 + x)^{\frac{1}{x}} = e$

47.-  $\lim_{x \rightarrow 0} \left( \frac{1}{x} - \frac{1}{\ln(x+1)} \right) = -\frac{1}{2}$

49.-  $\lim_{x \rightarrow 1} \left( \operatorname{tg}\left(\frac{p}{4}x\right) \right)^{\operatorname{tg}\left(\frac{p}{2}x\right)} = \frac{1}{e}$

51.-  $\lim_{x \rightarrow \infty} x^{\operatorname{sen}\frac{1}{x}} = 1$

53.-  $\lim_{x \rightarrow \infty} x \ln\left(\frac{x-a}{x+a}\right) = -2a$

55.-  $\lim_{x \rightarrow 0} \frac{(2-x)e^x - (2+x)}{x^2} = 0$

57.-  $\lim_{x \rightarrow \infty} (x + e^x + e^{2x})^{\frac{1}{x}} = e^2$

59.-  $\lim_{x \rightarrow 0} (1 + \operatorname{sen}x)^{\operatorname{cosec}(x/2)} = e^2$

61.-  $\lim_{x \rightarrow \infty} (1 - e^{-x})^x = \frac{1}{e}$

63.-  $\lim_{x \rightarrow 0} \frac{x - \operatorname{sen}2x}{x + \operatorname{sen}4x} = -\frac{1}{5}$

65.-  $\lim_{x \rightarrow 0} (1 - \operatorname{sen}2x)^{\operatorname{cotg}x} = 1$

46.-  $\lim_{x \rightarrow 0} (1 - \cos x)^{2x} = 1$

48.-  $\lim_{x \rightarrow 0} x^{\operatorname{sen}x} = 1$

50.-  $\lim_{x \rightarrow \frac{p}{2}} \left( \operatorname{tg}\left(\frac{x}{2}\right) \right)^{\frac{1}{x-p/2}} = 1$

52.-  $\lim_{x \rightarrow \frac{p}{2}} (1 - \cos x)^{\operatorname{tg}x} = \frac{1}{e}$

54.-  $\lim_{x \rightarrow 1} (1-x) \operatorname{tg}\left(\frac{p}{2}x\right) = \frac{2}{p}$

56.-  $\lim_{x \rightarrow 0} x \cdot \operatorname{sen}\frac{1}{x} = 0$

58.-  $\lim_{x \rightarrow p} (x-p) \operatorname{tg}\left(\frac{x}{2}\right) = -2$

60.-  $\lim_{x \rightarrow 0} (\operatorname{cotg}x)^x = 1$

62.-  $\lim_{x \rightarrow 0} (\operatorname{sen}x)^{\operatorname{tg}x} = 1$

64.-  $\lim_{x \rightarrow p} \frac{\operatorname{tg}x - x}{x - \operatorname{sen}x} = 0$

66.-  $\lim_{x \rightarrow 0} \frac{x - \operatorname{sen}x}{x^3} = \frac{1}{6}$

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